

The following choices will be used in this multiple choice problem:

- (a)  $\Theta(1)$
- (b)  $\Theta(\log n)$
- (c)  $\Theta(\sqrt{n})$
- (d)  $\Theta(n)$
- (e)  $\Theta(n \log n)$
- (f)  $\Theta(n^2)$
- (g)  $\Theta(n^3)$
- (h)  $\Theta(2^n)$

For each of the questions below, choose one of the above possible answers. Please write letter of your chosen answer to the left of the question.

- (a) Number of subsets of  $n$  elements *Solution:*  $\Theta(2^n)$
- (b) Maximum number of edges in an undirected graph over  $n$  nodes *Solution:*  $\Theta(n^2)$
- (c) Number of edges in a tree with  $n$  nodes *Solution:*  $\Theta(n)$
- (d) Fastest time to solve the single source shortest paths problem on a clique over  $n$  nodes with all positive edge weights *Solution:*  $\Theta(n^2)$
- (e) Fastest time to solve the single source shortest paths problem on a clique over  $n$  nodes with some negative edge weights *Solution:*  $\Theta(n^3)$
- (f) Total space required to represent a graph with  $n$  nodes and  $\Theta(n)$  edges using the adjacency matrix representation *Solution:*  $\Theta(n^2)$
- (g) Total space required to represent a graph with  $n$  nodes and  $\Theta(n)$  edges using the adjacency list representation *Solution:*  $\Theta(n)$
- (h) Solution to the recurrence  $T(1) = 1, T(n) = 2T(n/2) + n$  *Solution:*  $\Theta(n \log n)$
- (i) Solution to the recurrence  $T(1) = 1, T(n) = 2T(n/2) + n^2$  *Solution:*  $\Theta(n^2)$
- (j) Solution to the recurrence  $T(1) = 1, T(n) = 2T(n/2) + \log n$  *Solution:*  $\Theta(n)$