

# CS 261 HW4

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Due Weds, March 3

This homework covers material from Chapter 3.2 up to and including Chapter 3.6 in the textbook.

1. Prove that  $x^2 - 10x - 2$  is  $O(x^2)$ . Don't forget to solve for the correct values of  $c$  and  $n_0$ .
2. Explain what it means for a function to be  $\Omega(1)$
3. Exercise 3.2.60
4. Describe how the number of comparisons used in the worst case for BubbleSort changes when the size of the list to be sorted doubles from  $n$  to  $2n$
5. Prove or disprove that for integers if  $a|bc$  then  $a|b$  or  $a|c$  for integers  $a, b, c$ . (Be careful)
6. List 5 integers that are congruent to 1 modulo 12
7. Which of the following integers are congruent to 2 modulo 7? 2, 3, 16, 14, -2, -10
8. Find  $\gcd(123, 277)$  and  $\gcd(1349, 1786)$  using Euclid's algorithm - show your work
9. Decrypt the following message that was encrypted with a Caesar cypher: "ORJNER GUR JBBQ RYIRF!". Hint: One approach is to read the section on decryption of Caesar cyphers at the end of section 3.4 and try out the different possibilities.
10. Use Algorithm 5 in Section 3.6 to find  $7^{212}$  modulo 9. Show your work.
11. Prove that the product of any 4 consecutive integers is divisible by 12.