2. Floyd-Warshall

Recall that in the Floyd-Warshall algorithm, dist(u, v, r) is defined to be the shortest part from u to v where all intermediate vertices (if any) are numbered r or less. The follow recurrence is used to eventually compute dist(u, v, |V|) for all vertices u and v:

$$dist(u, v, r) = \left\{ \begin{array}{ll} w(u \rightarrow v) & \text{if } r = 0 \\ \min\{dist(u, v, r - 1), \\ dist(u, r, r - 1) + dist(r, v, r - 1)\} \end{array} \right. \text{otherwise} \label{eq:dist}$$

For the following graph, please fill in the distance arrays computed by Floyd-Warshall for values of r. In the distance arrays, let the row be the vertex the path starts at and the colube the vertex the path ends at.

r = 3:

