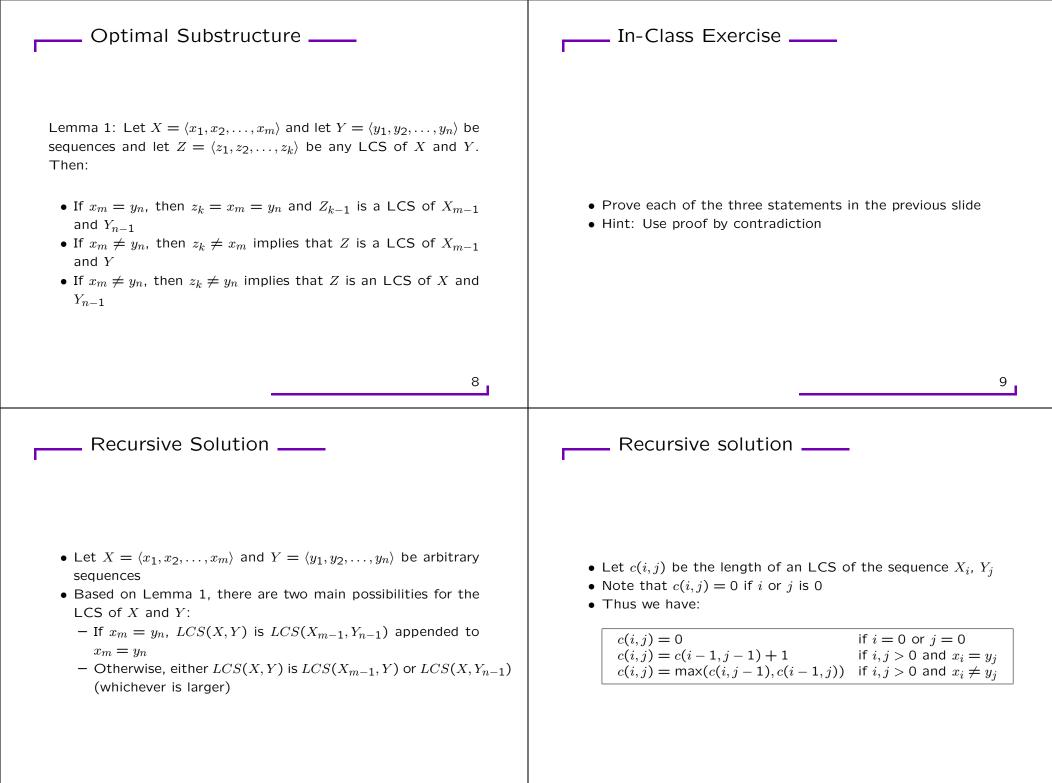


Common Subsequence _____ LCS Problem • Given two sequences X and Y, we say that Z is a common subsequence of X and Y if Z is a subsequence of X and Z is a subsequence of Y• We are given two sequences $X = \langle x_1, x_2, \dots, x_m \rangle$ and Y =• Example: $X = \langle A, B, D, C, B, A, B, C \rangle$, $Y = \langle A, D, B, C, D, B, A, B \rangle$ $\langle y_1, y_2, \ldots, y_n \rangle$ • Then $Z = \langle A, B, B, A, B \rangle$ is a common subsequence • Goal: Find a maximum-length common subsequence of X• Z is not a longest common subsequence(LCS) of X and Y and Ythough since the common subsequence $Z' = \langle A, B, C, B, A, B \rangle$ is longer • Q: Is Z' a longest common subsequence? 4 5 Brute Force _____ Terminology _____ • Brute Force approach is to enumerate all possible subsequences of X, check to see if its a subsequence of Y, and • Given a sequence $X = \langle x_1, x_2, \dots, x_m \rangle$, for $i = 0, 1, \dots, m$, let then keep track of the longest common subsequence of both X_i be the *i*-th prefix of X i.e. $X_i = \langle x_1, x_2, \dots, x_i \rangle$ X and Y• Example: if $X = \langle A, B, D, C \rangle$, $X_0 = \langle \rangle$ and $X_3 = \langle A, B, D \rangle$ • This is slow. • Q: How many subsequences of X are there?

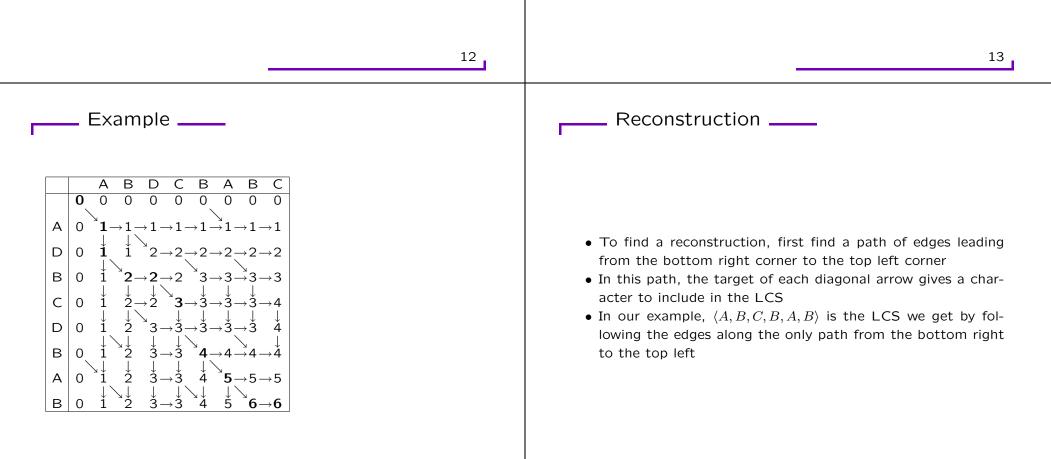


DP Solution _____

Example .	
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- This is already enough to write up a recursive function, however the naive recursive function will take exponential time
- Instead, we can use dynamic programming and solve from the bottom up
- Code for doing this is on p. 353 and 355 of the text, basically it uses the same ideas we've seen before of filling in entries in a table from the bottom up.

- Consider $X = \langle A, B, D, C, B, A, B, C \rangle$, $Y = \langle A, D, B, C, D, B, A, B \rangle$
- The next slide gives the table constructed by the DP algorithm for computing the LCS of X and Y
- The bold numbers represent one possible path giving a LCS.
- The arrows keep track of where the minimum is obtained from



Take Away _____

bottom up

Greedy Algorithms _____

"Greed is Good" - Michael Douglas- in Wall Street

- A greedy algorithm always makes the choice that looks best at the moment
- Greedy algorithms do not always lead to optimal solutions, but for many problems they do
- In the next week or two, we will see several problems for which greedy algorithms produce optimal solutions including: activity selection, fractional knapsack, and making change
- When we study graph theory, we will also see that greedy algorithms work well for computing shortest paths and finding minimum spanning trees.

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Activity Selection

• We've seen four different DP type algorithms

• In each case, we did the following 1) found a recurrence for

• You should be prepared to do this on your own now!

the solution 2) built solutions to the recurrence from the

- You are given a list of programs to run on a single processor
- Each program has a start time and a finish time
- However the processor can only run one program at any given time, and there is no preemption (i.e. once a program is running, it must be completed)

Another Motivating Problem _____

- Suppose you are at a film fest, all movies look equally good, and you want to see as many complete movies as possible
- This problem is also exactly the same as the activity selection problem.

